

Recent Progress on Curvature Squared Supergravities in Five and Six Dimensions

Mehmet Ozkan

in collaboration with
Yi Pang (Texas A&M University)

hep-th/1301.6622

April 24, 2013

- 1 Motivation and Background
- 2 Superconformal Multiplets in 5D
- 3 Off-Shell Poincaré Supergravities
- 4 All Higher Derivative Extensions of 5D Model
- 5 Ricci Scalar Squared Extended 6D Model
- 6 Summary

Higher Order Curvature Terms in Supergravity

String Theory

- At low energies, superstring theory reduce to supergravity
- Superstring actions originate higher curvature terms as well as Einstein-Hilbert supergravities

Supergravity

- Inclusion of Lorentz-Chern-Simons 3-form for the cancellation of anomalies in YM and gravitational gauge currents in 10D SUGRA coupled to YM [GS]
- Modify the definition of H

$$H = dB + (AF - A^3) - (R\omega - \omega^3)$$

Higher Order Curvature Terms in Supergravity

Restore Supersymmetry

- Supersymmetric completion of LCS term is needed
- String Theory: String amplitues in tree level and one loop level
- Supergravity: Superspace methods and Noether methods
- Result: $R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma}$

Problems

- Modified Lagrangian contains ghost particles [Siegel'84]
- Gauss - Bonnet combination is ghost free [Zwiebach '85]

$$e^{-1}\mathcal{L} = R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma} - 4R_{\mu\nu}R^{\mu\nu} + R^2$$

- Modifications to vacuum solutions?

Higher Order Curvature Terms in Supergravity

Solution

- String theory is **on-shell!**

Field Redefinition

- Higher curvature terms take the form of infinite series expansion as the on-shell supersymmetry works only order by order
- Only the coefficient of $R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma}$ has a definite meaning
- A field redefinition is always possible
 - $g'_{\mu\nu} = g_{\mu\nu} + aR_{\mu\nu} + bg_{\mu\nu}R$
 - Can shift the coefficients of $R_{\mu\nu}R^{\mu\nu}$ and R^2 to arbitrary values

Exact Supersymmetric Models

- **Off-shell** formulations needed
- Full answer to exact supersymmetric models was achieved in $D = 4, N = 1$
- $Riem^2$ action was constructed in 5 and 6 dimensions
- $Weyl^2$ action was constructed in 5 dimensions

More Motivation

- Higher order effects in AdS/CFT
- Corrections to black hole entropy

Today's Objectives

- Off-shell Poincaré Supergavities in Five Dimensions
- All supersymmetric curvature squared invariants in Five Dimensions
- Off-shell R^2 invariant in Six Dimensions
- Brief discussion on supersymmetric $f(R)$ theory

Current Status

Status of $D = 5$, $\mathcal{N} = 2$ Supergravity

- Off-Shell Poincaré Supergravity
[Bergshoeff et. al., Fujita & Ohashi, Zucker, Coomans & Ozkan]
- Off-Shell Weyl Squared Invariant
[Hanaki, Ohashi & Tachikawa]
- Off-Shell Riemann Squared Invariant
[Bergshoeff, Rosseel & Sezgin]

Status of $D = 6$, $\mathcal{N} = (1, 0)$ Supergravity

- Off-Shell Poincaré Supergravity
[Bergshoeff, van Proeyen & Sezgin]
- Off-Shell Riemann Squared Invariant
[Bergshoeff, Salam & Sezgin]

Superconformal Tensor Calculus

Toy Model: Proca Action from a $U(1)$ Invariant Action

Proca Action

- Proca Action

$$e^{-1} \mathcal{L}_{Proca} = -\frac{1}{4} G_{\mu\nu} G^{\mu\nu} - \frac{1}{2} m^2 C_\mu C^\mu$$

- Mass term forbids the local $U(1)$ symmetry

$U(1)$ Invariant Action

- Introduce a compensating scalar

$$\delta_\Lambda \sigma = m\Lambda$$

- Redefine the Proca field

$$C_\mu = A_\mu - m^{-1} \partial_\mu \sigma, \quad \delta_\Lambda A_\mu = \partial_\mu \Lambda$$

Toy Model: Proca Action from a $U(1)$ Invariant Action

$U(1)$ Invariant Action

- $U(1)$ invariant action

$$e^{-1}\mathcal{L}_{U(1)} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{1}{2}D_{\mu}\sigma D^{\mu}\sigma,$$

where

$$D_{\mu}\sigma = \partial_{\mu}\sigma - mA_{\mu}$$

- Fix $U(1)$ symmetry via $\sigma = 0 \rightarrow$ Proca action

Superconformal Multiplets

Weyl Multiplets of $\mathcal{N} = 2$ Supergravity in Five Dimensions

$\mathcal{N} = 2$, $D = 5$ Superconformal tensor calculus is based on the superconformal algebra $F^2(4)$

Generators and Gauge Fields

P_a	e_μ^a	Translations
M_{ab}	ω_μ^{ab}	Rotations
D	b_μ	Dilatations
K_a	f_a^μ	Special conformal
Λ^{ij}	V_μ^{ij}	$SU(2)$ R-Symmetry
Q^i	ψ_μ^i	Susy
S^i	ϕ_μ^i	S-Susy

Weyl Multiplets of $\mathcal{N} = 2$ Supergravity in Five Dimensions

Conventional Constraints

$$\begin{array}{l|l} R_{\mu\nu}(P^a) = 0 & \text{Identifies } \omega_{\mu}{}^{ab} \\ e^{\nu}{}_{b}\hat{R}_{\mu\nu}(M^{ab}) = 0 & \text{Identifies } f_{\mu}{}^a \\ \gamma^{\mu}\hat{R}_{\mu\nu}^i(Q) = 0 & \text{Identifies } \phi_{\mu}^i \end{array}$$

Independent Gauge Fields

$$e_{\mu}{}^a \quad b_{\mu} \quad \psi_{\mu}^i \quad V_{\mu}{}^{ij}$$

- Independent gauge fields have 21(bosonic) + 24 (fermionic) degrees of freedom. Cannot represent a superconformal multiplet

Weyl Multiplets of $\mathcal{N} = 2$ Supergravity in Five Dimensions

Additional matter **fields** must be added to gauge fields in order to obtain an off-shell closed multiplet

- There are two choices [Bergshoeff et al]

Standard Weyl Multiplet

$$e_\mu^a \quad b_\mu \quad \psi_\mu^i \quad V_\mu^{ij} \quad T_{\mu\nu}(10) \quad D(1) \quad \chi^i(8)$$

Dilaton Weyl Multiplet

$$e_\mu^a \quad b_\mu \quad \psi_\mu^i \quad V_\mu^{ij} \quad B_{\mu\nu}(6) \quad C_\mu(4) \quad \sigma(1) \quad \psi^i(8)$$

Construction of an off-shell Gauss - Bonnet combination requires **Dilaton Weyl Multiplet**

Weyl Multiplets of $\mathcal{N} = 2$ Supergravity in Five Dimensions

Map Between the Weyl Multiplet

$$\chi^i = \frac{1}{8}i\sigma^{-1}\not{D}\psi^i + \frac{1}{16}i\sigma^{-2}\not{D}\sigma\psi^i - \frac{1}{32}\sigma^{-2}\gamma \cdot G\psi^i + \dots$$

$$D = -\frac{1}{32}R + \frac{1}{8}\sigma^{-2}\partial_\mu\sigma\partial^\mu\sigma - \frac{1}{16}\sigma^{-2}G_{\mu\nu}G^{\mu\nu} + \dots$$

$$T_{ab} = \frac{1}{8}\sigma^{-1}G_{ab} + \frac{1}{48}\sigma^{-2}\varepsilon_{abcde}H^{cde} + \dots$$

Compensating Multiplets: The Vector Multiplet

Vector Multiplet

Field	Weyl Weight
A_μ	0
ρ	1
Y^{ij}	2
λ^i	$\frac{3}{2}$

- Contains a gauge field A_μ with gauge invariance $\partial_\mu \Lambda$
- Scalar is S-invariant $\delta_S \rho = 0$

Compensating Multiplets: The Linear Multiplet

Linear Multiplet

Field	Weyl Weight
L_{ij}	3
φ^i	$\frac{7}{2}$
E_a	4
N	4

- Contains a conserved current $\mathcal{D}^a E_a = 0$
- $E^a = -\frac{1}{12} e_\mu{}^a e^{-1} \varepsilon^{\mu\nu\rho\sigma\lambda} \mathcal{D}_\nu E_{\rho\sigma\lambda}$
- Invariant Action Formula: $e^{-1} \mathcal{L}_{VL} = Y_{ij} L^{ij} + \rho N + A^a E_a$

Intermezzo: How to construct off-shell actions?

Vector - Linear Action

- $e^{-1}\mathcal{L}_{VL} = Y_{ij}L^{ij} + \rho N + A^a P_a$

Embedding Formulae

- Define the elements of Vector (or Linear) multiplet in terms of other multiplets
- Use these expressions in the Vector - Linear action (or any other superconformal action) to obtain a superconformal action
- Fix the redundant superconformal symmetries

Off-Shell Poincaré Supergravity

Construction of the Linear Multiplet Action

Identify the elements of Vector Multiplet in terms of Linear Multiplet

Step 1: Composite expressions for ρ , λ_i , Y_{ij} and $\widehat{F}_{\mu\nu}$

$$\rho = 2L^{-1}N + iL^{-3}L_{ij}\bar{\varphi}^i\varphi^j$$

$$\lambda_i = \dots$$

$$Y_{ij} = L^{-1}\square^C L_{ij} - \mathcal{D}_a L_{k(i}\mathcal{D}^a L_{j)k}L^{km}L^{-3} - N^2 L_{ij}L^{-3} - E_\mu E^\mu L_{ij}L^{-3} \\ + \frac{8}{3}T^2 L^{-1}L_{ij} + 4L^{-1}DL_{ij} + 2E_\mu L_{k(i}\mathcal{D}^\mu L_{j)}^k L^{-3} + \dots$$

$$\widehat{F}_{\mu\nu} = 4\mathcal{D}_{[\mu}(L^{-1}E_{\nu]}) + 2L^{-1}\widehat{R}_{\mu\nu}{}^{ij}(V)L_{ij} - 2L^{-3}L_k^l \mathcal{D}_{[\mu}L^{kp}\mathcal{D}_{\nu]}L_{lp} + \dots$$

Construction of the Linear Multiplet Action

Construct a superconformal action

Step 2: Use \mathcal{L}_{VL} to construct Linear Multiplet action

$$\begin{aligned} e^{-1}\mathcal{L}_L = & L^{-1}L_{ij}\square^C L^{ij} - L^{ij}\mathcal{D}_a L_{k(i}\mathcal{D}^a L_{j)k}L^{km}L^{-3} - N^2L^{-1} - E_\mu E^\mu L^{-1} \\ & + \frac{8}{3}LT^2 + 4DL - \frac{1}{2}L^{-3}E^{\mu\nu}L_k^l\partial_\mu L^{kp}\partial_\nu L_{pl} \\ & + 2E^{\mu\nu}\partial_\mu(L^{-1}E_\nu + V_\nu^{ij}L_{ij}L^{-1}) \end{aligned}$$

- $L_{ij}\square^C L^{ij} = L_{ij}\square L^{ij} - \frac{3}{8}L^2R$
- $D = -\frac{1}{32}R + \dots$
- **Can** describe a consistent Poincaré supergravity upon gauge fixing

Construction of the Poincaré Theory

Gauge Fixing

$$\begin{array}{l|l} L_{ij} = -\frac{1}{\sqrt{2}}\delta_{ij}L & \text{Breaks } SU(2) \text{ to } U(1)_R \\ \sigma = 1 & \text{Dilatation} \\ b_\mu = 0 & \text{Conformal boost} \\ \psi^i = 0 & \text{S - Supersymmetry} \end{array}$$

Off-Shell Poincaré Supergravity

$$\begin{aligned} e^{-1}\mathcal{L}_{LR}|_{\sigma=1} &= \frac{1}{2}LR - \frac{1}{4}LG_{\mu\nu}G^{\mu\nu} - \frac{1}{6}LH_{\mu\nu\rho}H^{\mu\nu\rho} - \frac{1}{2}L^{-1}\partial_\mu L\partial^\mu L \\ &+ L^{-1}N^2 - L^{-1}E_\mu E^\mu + \sqrt{2}E_\mu V^\mu + LV'_\mu{}^{ij}V'_{ij}{}^\mu \end{aligned}$$

Construction of the Poincaré Theory

Remarks

- Decomposed $V_\mu{}^{ij}$ into its trace and traceless part

$$V_\mu{}^{ij} = V_\mu{}'ij + \frac{1}{\sqrt{2}} V_\mu \delta_{ij}, \quad V_\mu{}'ij \delta_{ij} = 0$$

- $U(1)_R$ symmetry is gauged by the auxiliary V_μ
- Corresponding on-shell theory is the Ungauged Maxwell - Einstein theory [Gunaydin - Sierra - Townsend]

Off-Shell Higher Derivative Extensions

- Riemann Squared Invariant [Bergshoeff - Rosseel - Sezgin]
- Weyl Tensor Squared Invariant [$C_{\mu\nu\rho\sigma}C^{\mu\nu\rho\sigma} + \frac{1}{6}R^2$]
- Ricci Scalar Squared Invariant

Construction of the Riemann Squared Action

Riemann Squared Action - Key Observation

- Based on a map between the Yang - Mills multiplet and Dilaton Weyl multiplet

Riemann Squared Action - Construction Procedure Step 1:

- Establish a map between the Yang-Mills multiplet and Dilaton Weyl multiplet [Bergshoeff - Rosseel - Sezgin '11]

$$\left(A_{\mu}^I Y_{I}^{ij}, \lambda_{I}^i, \rho_I \right) \longleftrightarrow \left(\widehat{\omega}_{+\mu}^{ab}, -\widehat{V}_{ab}^{ij}, -\widehat{\psi}_{ab}^i, \widehat{G}_{ab} \right)$$

- $\widehat{\omega}_{+\mu}^{ab}$ is torsionful spin connection

$$\widehat{\omega}_{+\mu}^{ab} = \omega_{\mu}^{ab} + \widehat{H}_{\mu}^{ab}$$

Construction of the Riemann Squared Action

Step 2: Construction of the Yang-Mills Action

- Linear Multiplet \rightarrow Dilaton Weyl Multiplet \times Yang-Mills Multiplet

$$L_{ij} = \sigma Y_{ij} + \dots$$

$$\varphi_i = \frac{1}{2} i \sigma \not{D} \lambda_i + \dots$$

$$E^a = D_b \left(-\frac{1}{2} \sigma \widehat{F}^{ab} + \dots \right) - \frac{1}{8} \epsilon^{abcde} G_{bc} F_{de}$$

$$N = \frac{1}{2} \rho \square^c \sigma + \frac{1}{2} \sigma \square^c \rho - 4 \sigma \rho D + \dots$$

- Use \mathcal{L}_{VL}

$$\begin{aligned} e^{-1} \mathcal{L}_{YM} = & a_{IJ} \left(\sigma Y_{ij}^I Y^{ijJ} - \frac{1}{4} \sigma F_{\mu\nu}^I F^{\mu\nu J} - \frac{1}{2} \rho^I F_{\mu\nu}^J G^{\mu\nu} - 8 \sigma \rho^I F_{\mu\nu} T^{\mu\nu} \right. \\ & + \frac{1}{2} \rho^I \rho^J \square^C \sigma + \frac{1}{2} \sigma \rho^I \square^C \rho^J + \frac{1}{2} \rho^I D_a \rho^J D^a \sigma - 4 \sigma \rho^I \rho^J \left(D + \frac{26}{3} T^2 \right) \\ & \left. + 4 \rho^I \rho^J G_{\mu\nu} T^{\mu\nu} - \frac{1}{8} \epsilon^{\mu\nu\rho\sigma\lambda} F_{\mu\nu}^I F_{\rho\sigma}^J C_\lambda \right) \end{aligned}$$

Construction of the Riemann Squared Action

Step 3: Gauge Fix the Yang-Mills action and use the map

- Bosonic part of the Riemann tensor squared action

$$\begin{aligned} e^{-1} \mathcal{L}_{Riem^2} = & -\frac{1}{4} \left(R_{\mu\nu ab}(\omega_+) - G_{\mu\nu} G_{ab} \right) \left(R^{\mu\nu ab}(\omega_+) - G^{\mu\nu} G^{ab} \right) \\ & + \frac{1}{2} \nabla_\mu(\omega_+) G^{ab} \nabla^\mu(\omega_+) G_{ab} + V_{\mu\nu}{}^{ij} V^{\mu\nu}{}_{ij} \\ & - \frac{1}{8} \epsilon^{\mu\nu\rho\sigma\lambda} \left(R_{\mu\nu ab}(\omega_+) - G_{\mu\nu} G_{ab} \right) \left(R_{\rho\sigma ab}(\omega_+) - G_{\rho\sigma} G_{ab} \right) C_\lambda \\ & - \frac{1}{2} \epsilon^{\mu\nu\rho\sigma\lambda} B_{\rho\sigma} \left(R_{\mu\nu ab}(\omega_+) - G_{\mu\nu} G_{ab} \right) \left(R_{\rho\sigma ab}(\omega_+) - G_{\rho\sigma} G_{ab} \right) \nabla_\lambda(\omega_+) G^{ab} \end{aligned}$$

- $V_{\mu\nu}{}^{ij} V^{\mu\nu}{}_{ij}$ - Kinetic term for the auxiliary V_μ^{ij}
- Massive particles in the spectrum

What do we know so far?

- Off-shell Poincaré supergravity in $\sigma = 1$ gauge fixing condition
- Riemann squared invariant in $\sigma = 1$ gauge fixing
 - Riemann squared term generates massive graviton
 - Auxiliary vector V_μ becomes dynamical, and generates massive dynamical auxiliary vector

Key Observation

- Massive graviton and massive auxiliary vector falls into same multiplet

Construction of Gauss-Bonnet Combination: The Idea

Key Idea

- Construct a new higher derivative invariant
- Combine two off-shell higher derivative invariants \Rightarrow Vanishing $V_{\mu\nu}{}^{ij}$
- Massive multiplet decouples
- Gauss - Bonnet combination

Weyl Tensor Squared Invariant

- Weyl tensor square

$$C_{\mu\nu\rho\sigma} C^{\mu\nu\rho\sigma} = R_{\mu\nu\rho\sigma} R^{\mu\nu\rho\sigma} - \frac{4}{3} R_{\mu\nu} R^{\mu\nu} + \frac{1}{6} R^2$$

- Gauss-Bonnet requires $C_{\mu\nu\rho\sigma} C^{\mu\nu\rho\sigma} + \frac{1}{6} R^2$
- In superconformal language,

$$\widehat{C}_{\mu\nu\rho\sigma} \widehat{C}^{\mu\nu\rho\sigma} + \frac{512}{3} D^2$$

- **Claim:** If the supersymmetrization of Weyl tensor square includes $V_{\mu\nu}{}^{ij}$ then it has to include $\frac{512}{3} D^2$

Weyl Tensor Squared Invariant

- Linear Multiplet \rightarrow Dilaton Weyl Multiplet

$$L^{ij} = \frac{1}{4} i \bar{\hat{R}}_{ab}^{(i}(Q) \hat{R}^{j)ab}(Q) + \frac{256}{3} i \bar{\chi}^{(i} \chi^{j)} + \frac{16}{3} \hat{R}_{ab}{}^{ij}(V) T^{ab}$$

$$\varphi^i = -\frac{1}{8} \gamma_{cd} \hat{R}_{ab}^i(Q) \hat{C}^{abcd} + \dots$$

$$E^a = \frac{1}{16} \epsilon_{abcde} \hat{C}^{bcfg} \hat{C}^{de}_{fg} + \dots$$

$$N = \frac{1}{8} \hat{C}_{abcd} \hat{C}^{abcd} + \frac{64}{3} D^2 - \frac{1}{3} \hat{V}_{ab}{}^{ij} \hat{V}^{ab}{}_{ij} + \dots$$

Weyl Tensor Squared Invariant

- Use \mathcal{L}_{VL}

$$e^{-1}\mathcal{L}_{\rho R^2} = +\frac{1}{8}\rho C_{\mu\nu\rho\sigma}C^{\mu\nu\rho\sigma} + \frac{64}{3}\rho D^2 - \frac{1}{3}\rho V_{ab}{}^{ij}V^{ab}{}_{ij} \\ + \frac{1}{16}\epsilon_{abcde}A^a C^{bcfg}C^{de}{}_{fg} + \dots$$

- **Problem**
 - Riemann² is written purely in terms of Dilaton Weyl multiplet
 - Weyl² uses both Dilaton Weyl multiplet and Vector multiplet
 - Need a map: **Vector multiplet** \rightarrow **Dilaton Weyl multiplet**

Construction of Gauss-Bonnet Combination

Vector multiplet \rightarrow Dilaton Weyl multiplet

$$\left(A_\mu, Y^{ij}, \lambda^i, \rho \right) \rightarrow \left(C_\mu, \frac{1}{4} i \sigma^{-1} \bar{\psi}^i \psi^j, \psi^i, \sigma \right)$$

$$e^{-1} \mathcal{L}_{\sigma R^2} |_{\sigma=1} = +\frac{1}{8} C_{\mu\nu\rho\sigma} C^{\mu\nu\rho\sigma} + \frac{64}{3} D^2 - \frac{1}{3} V_{ab}{}^{ij} V^{ab}{}_{ij} \\ + \frac{1}{16} \epsilon_{abcde} C^a{}^{bcfg} C^{de}{}_{fg} + \dots$$

Off-Shell Theory

$$\begin{aligned} e^{-1}(\mathcal{L}_{LR} + \alpha\mathcal{L}_{R^2} + \beta\mathcal{L}_{W^2}) &= \frac{1}{2}LR + \frac{1}{2}L^{-1}\partial_\mu L\partial^\mu L - \frac{1}{4}LG_{\mu\nu}G^{\mu\nu} + \dots \\ &+ \alpha \left[-\frac{1}{4}R_{abcd}R^{abcd} + V_{ab}{}^{ij}V^{ab}{}_{ij} + \dots \right] \\ &+ \beta \left[\frac{1}{8}R_{abcd}R^{abcd} - \frac{1}{6}R_{ab}R^{ab} + \frac{1}{24}R^2 \right. \\ &\quad \left. - \frac{1}{3}V_{ab}{}^{ij}V^{ab}{}_{ij} + \dots \right] \end{aligned}$$

Gauss-Bonnet Combination

Gauss-Bonnet Combination

- Set $\beta = 3\alpha$ to obtain Gauss - Bonnet combination

$$e^{-1}(\mathcal{L}_{LR} + \alpha\mathcal{L}_{GB}) = \frac{1}{2}LR + \dots \\ + \frac{1}{8}\alpha(R_{abcd}R^{abcd} - 4R_{ab}R^{ab} + R^2 + \dots)$$

Remarks

- No kinetic term for the auxiliary $V_\mu{}^{ij}$
- Curvature terms read the Gauss-Bonnet combination
- Corresponding on-shell theory is the Gauss-Bonnet extended Einstein-Maxwell theory

Key Idea

- Define the elements of Vector (or Linear) multiplet in terms of other multiplets
- Use these expressions in the Vector - Linear action (**or any other superconformal action**) to obtain a superconformal action
- Fix the redundant superconformal symmetries

Ricci Scalar Squared Action

- Use the composite linear multiplet fields in vector multiplet action

$$Y_{ij} = L^{-1} \square^C L_{ij} - \mathcal{D}_a L_{k(i} \mathcal{D}^a L_{j)k} L^{km} L^{-3} - N^2 L_{ij} L^{-3} - E_\mu E^\mu L_{ij} L^{-3} \\ + \frac{8}{3} T^2 L^{-1} L_{ij} + 4L^{-1} D L_{ij} + 2E_\mu L_{k(i} \mathcal{D}^\mu L_{j)}^k L^{-3} + \dots$$

- $e^{-1} \mathcal{L}_{R^2} = \frac{1}{4} R^2 + (H^2)^2 + (E^2)^2 + \dots$

Summary

Summary

	Poincaré	Riem ²	Weyl ² + R ²	R ²	R ² _{ab}
5D	✓	✓	✓	✓	✓
6D	✓	✓	In Progress	✓	

Outlook

- No AdS_5 solution \rightarrow Gauging
- Generalize to $D = 6$, $\mathcal{N} = (1, 0)$ theory, and reduction to $D = 4$, $\mathcal{N} = 2$ theory
- Higher order effects in AdS/CFT correspondence
- Corrections to black hole entropies

Thank you!